

Haskell Programming Assignment: Various Computations

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Learning Abstract

This assignment played an important role in cultivating my understanding of Haskell. Throughout this assignment 8 tasks were completed each sequential task requiring slightly more knowledge of Haskell. Task 7 was my favorite task of this assignment, I got to use Haskell to build a mathematical function (nPVI) from the ground up.

Task 1 – Mindfully Mimicking the Demo

Demo

```
david@david-IdeaPad-1-15ALC7 ~ ➤ ghci
GHCi, version 8.8.4: https://www.haskell.org/ghc/  ?: for help
Prelude> :set prompt ">>> "
>>> length [2,3,5,7]
4
>>> words "need more coffee"
["need", "more", "coffee"]
>>> unwords ["need", "more", "coffee"]
"need more coffee"
>>> reverse "need more coffee"
"eefhoc erom deen"
>>> reverse ["need", "more", "coffee"]
["coffee", "more", "need"]
>>> head ["need", "more", "coffee"]
"need"
>>> tail ["need", "more", "coffee"]
["more", "coffee"]
>>> last ["need", "more", "coffee"]
"coffee"
>>> init ["need", "more", "coffee"]
["need", "more"]
>>> take 7 "need more coffee"
"need mo"
>>> drop 7 "need more coffee"
"re coffee"
>>> ( \x -> length x > 5 ) "Friday"
True
>>> ( \x -> length x > 5 ) "uhoh"
False
>>> ( \x -> x /= ' ') 'Q'
True
>>> ( \x -> x /= ' ') ' '
False
>>> filter ( \x -> x /= ' ') "Is the Haskell fun yet?"
"IstheHaskellfunyet?"
>>> :quit
Leaving GHCi.
david@david-IdeaPad-1-15ALC7 ~ ➤ □
```

Task 2 – Numeric Function Definitions

Function Definitions

--- ha.hs houses task 2 of the haskell assignment

--- squareArea :: takes one real number representing the side length
--- of a square and returns the area of the square with the given side
--- length

squareArea x = x * x

--- circleArea :: takes one real number representing the radius of a circle
--- and returns the corresponding circles area

circleArea r = pi * r ^ 2

--- blueAreaOfCube :: takes the length of one edge of the cube and computes
--- the area of the cube that is equivalent to the cube's area minus a
--- centered dots area (on each side of the cube)
--- with a radius 1/4 the edges length.

blueAreaOfCube el = (6 * el ^ 2) - (6 * pi * (el / 4) ^ 2)

--- paintedCube1 :: takes the order of a n by n by n cube where n is

--- equal to order and returns the number of cubes that are painted once

--- when the entire cube is painted

paintedImage1 order = if order < 3 then 0 else $6 * ((\text{order} - 2) ^ 2)$

--- paintedImage2 :: takes the order of a n by n by n cube where n is equal

--- to order and returns the number of cubes that are painted twice when the

--- entire cube is painted

paintedImage2 order = if order < 3 then 0 else $12 * (\text{order} - 2)$

Demo

```
david@david-IdeaPad-1-15ALC7 ~/repos/CSC344/assignments ghci
GHCi, version 8.8.4: https://www.haskell.org/ghc/ :? for help
Prelude> :set prompt ">>> "
>>> :load ha.hs
[1 of 1] Compiling Main           ( ha.hs, interpreted )
Ok, one module loaded.
>>> squareArea 10
100
>>> squareArea 12
144
>>> circleArea 10
314.1592653589793
>>> circleArea 12
452.3893421169302
>>> blueAreaOfCube 10
482.19027549038276
>>> blueAreaOfCube 12
694.3539967061512
>>> blueAreaOfCube 1
4.821902754903828
>>> map blueAreaOfCube [1..3]
[4.821902754903828,19.287611019615312,43.39712479413445]
>>> paintedImage1 1
0
>>> paintedImage1 2
0
>>> paintedImage1 3
6
>>> map paintedImage1 [1..10]
[0,0,6,24,54,96,150,216,294,384]
>>> paintedImage2 1
0
>>> paintedImage2 2
0
>>> paintedImage2 3
12
>>> map paintedImage2 [1..10]
[0,0,12,24,36,48,60,72,84,96]
>>> :quit
Leaving GHCi.
david@david-IdeaPad-1-15ALC7 ~/repos/CSC344/assignments □
```

Task 3 – Puzzlers

Function Definitions

--- reverseWords :: reverses the words of a string

```
reverseWords wordString = unwords ( reverse ( words wordString ) )
```

--- averageWordLength :: takes a string of words and returns the average

--- word length

```
averageWordLength wordString = fromIntegral ( sum letterCountList ) / fromIntegral wordCount
```

where wordList = words wordString

wordCount = length wordList

letterCountList = map length wordList

Demo

```
david@david-IdeaPad-1-15ALC7 ~/repos/CSC344/assignments ghci
GHCi, version 8.8.4: https://www.haskell.org/ghc/ :? for help
Prelude> :set prompt ">>> "
>>> :l ha.hs
[1 of 1] Compiling Main           ( ha.hs, interpreted )
Ok, one module loaded.
>>> reverseWords "appa and baby yoda are the best"
"best the are yoda baby and appa"
>>> reverseWords "want me some coffee"
"coffee some me want"
>>> reverseWords "haskell is fun"
"fun is haskell"
>>> reverseWords "I enjoy listening to Chopin"
"Chopin to listening enjoy I"
>>> averageWordLength "appa and baby yoda are the best"
3.5714285714285716
>>> averageWordLength "want me some coffee"
4.0
>>> averageWordLength "haskell is fun"
4.0
>>> averageWordLength "I enjoy listening to Chopin"
4.6
>>> :quit
Leaving GHCi.
david@david-IdeaPad-1-15ALC7 ~/repos/CSC344/assignments □
```

Task 4 – Recursive List Processors

Function Definitions

--- list2set :: takes a list and turns it into a set

```
list2set l = if (length l) == 0 then [] else (if elem (head l) set then set else (head l) : set)
```

where set = list2set(tail l)

--- isPalindrome :: checks to see if a list is a palindrome

```
isPalindrome l = if (length l) < 2 then True else (if (head l) == (last l) then (isPalindrome (tail (init l)))  
else False)
```

--- collatz :: takes a number as an input and generates a list containing

--- the corresponding collatz sequence

```
collatz :: Integer -> [Integer]
```

```
collatz num = if num == 1 then [1] else ( num : l )
```

where nextNum = if (rem num 2) == 0 then (div num 2) else (3 * num + 1)

```
l = ( collatz nextNum )
```

Demo

```
david@david-IdeaPad-1-15ALC7 > ~/repos/CSC344/assignments ➤ ghci
GHCi, version 8.8.4: https://www.haskell.org/ghc/  :? for help
Prelude> :set prompt ">>> "
>>> :l ha.hs
[1 of 1] Compiling Main           ( ha.hs, interpreted )
Ok, one module loaded.
>>> list2set [1,2,3,2,3,4,3,4,5]
[1,2,3,4,5]
>>> list2set "need more coffee"
"ndmr cofe"
>>> isPalindrome ["coffee","latte","coffee"]
True
>>> isPalindrome ["coffee","latte","espresso","coffee"]
False
>>> isPalindrome [1,2,5,7,11,13,11,7,5,3,2]
False
>>> isPalindrome [2,3,5,7,11,13,11,7,5,3,2]
True
>>> collatz 10
[10,5,16,8,4,2,1]
>>> collatz 11
[11,34,17,52,26,13,40,20,10,5,16,8,4,2,1]
>>> collatz 100
[100,50,25,76,38,19,58,29,88,44,22,11,34,17,52,26,13,40,20,10,5,16,8,4,2,1]
>>> :quit
Leaving GHCi.
david@david-IdeaPad-1-15ALC7 > ~/repos/CSC344/assignments ➤ ┡
```

Task 5 – List Comprehensions

Function Definitions

--- count :: takes an object and a list of objects then returns the amount

--- of times the object appears within the list.

count object objects = length [x | x <- objects, x == object]

--- freqTable :: takes a list of objects and returns a list of ordered

--- pairs each consisting of an element of the list together with the number

--- of times it occurred

```
freqTable objects = [ (x,y) | x <- (list2set objects), y <- [(count x objects)]]
```

Demo

```
david@david-IdeaPad-1-15ALC7 ~/repos/CSC344/assignments ghci
GHCi, version 8.8.4: https://www.haskell.org/ghc/ :? for help
Prelude> :set prompt ">>> "
>>> :load ha.hs
[1 of 1] Compiling Main           ( ha.hs, interpreted )
Ok, one module loaded.
>>> count 'e' "need more coffee"
5
>>> count 4 [1,2,3,2,3,4,3,4,5,4,5,6]
3
>>> count 'a' "lambdas are rad"
4
>>> count 17 [17,3,5,7,9,17,4]
2
>>> freqTable "need more coffee"
[('n',1),('d',1),('m',1),('r',1),(' ',2),('c',1),('o',2),('f',2),('e',5)]
>>> freqTable [1,2,3,2,3,4,3,4,5,4,5,6]
[(1,1),(2,2),(3,3),(4,3),(5,2),(6,1)]
>>> freqTable "lambdas are rad"
[('l',1),('m',1),('b',1),('s',1),('e',1),(' ',2),('r',2),('a',4),('d',2)]
>>> freqTable [17,3,5,7,9,17,4]
[(3,1),(5,1),(7,1),(9,1),(17,2),(4,1)]
>>> :quit
Leaving GHCi.
```

Task 6 – Higher Order Functions

Function Definitions

--- vowelCount :: takes a string of lower case letters and returns the number

--- of lowercase vowels that appear in the string

```
vowelCount str = length (filter (\x -> (x == 'a' || x == 'e' || x == 'i' ||
```

```
x == 'o' || x == 'u')) str)
```

--- lcsim :: takes a function for mapping, a predicate for filtering, and
--- a list of elements and returns the same value as:
--- [f x | x <- xs, p x]

lcsim mapFunc pred elems = map (mapFunc) (filter (pred) elems)

Demo

```
david@david-IdeaPad-1-15ALC7 ~/repos/CSC344/assignments> ghci
GHCi, version 8.8.4: https://www.haskell.org/ghc/  ?: for help
Prelude> :set prompt ">>> "
>>> :load ha.hs
[1 of 1] Compiling Main           ( ha.hs, interpreted )
Ok, one module loaded.
>>> tgl 5
15
>>> tgl 10
55
>>> tgl 47
1128
>>> tgl 20
210
>>> triangleSequence 10
[1,3,6,10,15,21,28,36,45,55]
>>> triangleSequence 20
[1,3,6,10,15,21,28,36,45,55,66,78,91,105,120,136,153,171,190,210]
>>> triangleSequence 47
[1,3,6,10,15,21,28,36,45,55,66,78,91,105,120,136,153,171,190,210,231,253,276,300,325,351,378,406,435,465,496,528,561,595,630,
666,703,741,780,820,861,903,946,990,1035,1081,1128]
>>> triangleSequence 5
[1,3,6,10,15]
>>> vowelCount "cat"
1
>>> vowelCount "mouse"
3
>>> vowelCount "rat"
1
>>> vowelCount "lambda"
2
>>> lcsim tgl odd [1..15]
[1,6,15,28,45,66,91,120]
>>> animals = ["elephant","lion","tiger","orangutan","jaguar"]
>>> lcsim length (\w -> elem ( head w ) "aeiou") animals
[8,9]
>>> lcsim tgl even [1..15]
[3,10,21,36,55,78,105]
>>> lcsim length (\w -> elem ( head w ) "t") animals
[5]
>>> :quit
Leaving GHCi.
david@david-IdeaPad-1-15ALC7 ~/repos/CSC344/assignments>
```

Task 7 – An Interesting Statistic: nPVI

Task 7a – Test data

Function Definitions

--- Test data

a :: [Int]

a = [2,5,1,3]

b :: [Int]

b = [1,3,6,2,5]

c :: [Int]

c = [4,4,2,1,1,2,2,4,4,8]

u :: [Int]

u = [2,2,2,2,2,2,2,2,2]

x :: [Int]

x = [1,9,2,8,3,7,2,8,1,9]

Demo

```
>>> a  
[2,5,1,3]  
>>> b  
[1,3,6,2,5]  
>>> c  
[4,4,2,1,1,2,2,4,4,8]  
>>> u  
[2,2,2,2,2,2,2,2,2,2]  
>>> x  
[1,9,2,8,3,7,2,8,1,9]  
>>> 
```

Task 7b – The pairwiseValues function

Function Definitions

--- pairwiseValues

```
pairwiseValues :: [Int] -> [(Int,Int)]
```

```
pairwiseValues listOfInts = zip (init listOfInts) (tail listOfInts)
```

Demo

```
>>> pairwiseValues a  
[(2,5),(5,1),(1,3)]  
>>> pairwiseValues b  
[(1,3),(3,6),(6,2),(2,5)]  
>>> pairwiseValues c  
[(4,4),(4,2),(2,1),(1,1),(1,2),(2,2),(2,4),(4,4),(4,8)]  
>>> pairwiseValues u  
[(2,2),(2,2),(2,2),(2,2),(2,2),(2,2),(2,2),(2,2),(2,2)]  
>>> pairwiseValues x  
[(1,9),(9,2),(2,8),(8,3),(3,7),(7,2),(2,8),(8,1),(1,9)]  
>>> □
```

Task 7c – The pairwiseDifferences function

Function Definitions

--- pairwiseDifferences

```
pairwiseDifferences :: [Int] -> [Int]
```

```
pairwiseDifferences listOfElements = map (\(x,y) -> x - y ) (pairwiseValues listOfElements)
```

Demo

```
>>> pairwiseDifferences a  
[-3,4,-2]  
>>> pairwiseDifferences b  
[-2,-3,4,-3]  
>>> pairwiseDifferences c  
[0,2,1,0,-1,0,-2,0,-4]  
>>> pairwiseDifferences u  
[0,0,0,0,0,0,0,0,0]  
>>> pairwiseDifferences x  
[-8,7,-6,5,-4,5,-6,7,-8]  
>>>
```

Task 7d – The pairwiseSums function

Function Definitions

```
--- pairwiseSums
```

```
pairwiseSums :: [Int] -> [Int]
```

```
pairwiseSums listOfElements = map (\(x,y) -> x + y ) (pairwiseValues listOfElements)
```

Demo

```
>>> pairwiseSums a  
[7,6,4]  
>>> pairwiseSums b  
[4,9,8,7]  
>>> pairwiseSums c  
[8,6,3,2,3,4,6,8,12]  
>>> pairwiseSums u  
[4,4,4,4,4,4,4,4]  
>>> pairwiseSums x  
[10,11,10,11,10,9,10,9,10]  
>>> □
```

Task 7e – The pairwiseHalves function

Function Definitions

--- half

half :: Int -> Double

half number = (fromIntegral number) / 2

--- pairwiseHalves

pairwiseHalves :: [Int] -> [Double]

pairwiseHalves numbers = map (half) numbers

Demo

```
david@david-IdeaPad-1-15ALC7 ~/repos/CSC344/assignments ghci
GHCi, version 8.8.4: https://www.haskell.org/ghc/ ?: for help
Prelude> :set prompt ">>> "
>>> :load npvi.hs
[1 of 1] Compiling Main           ( npvi.hs, interpreted )
ok, one module loaded.
>>> pairwiseHalves [1..10]
[0.5,1.0,1.5,2.0,2.5,3.0,3.5,4.0,4.5,5.0]
>>> pairwiseHalves u
[1.0,1.0,1.0,1.0,1.0,1.0,1.0,1.0,1.0,1.0]
>>> pairwiseHalves x
[0.5,4.5,1.0,4.0,1.5,3.5,1.0,4.0,0.5,4.5]
>>> □
```

Task 7f – The pairwiseHalfSums function

Function Definition

--- pairwiseHalfSums

pairwiseHalfSums :: [Int] -> [Double]

pairwiseHalfSums numbers = pairwiseHalves (pairwiseSums numbers)

Demo

```
>>> pairwiseHalfSums a  
[3.5,3.0,2.0]  
>>> pairwiseHalfSums b  
[2.0,4.5,4.0,3.5]  
>>> pairwiseHalfSums c  
[4.0,3.0,1.5,1.0,1.5,2.0,3.0,4.0,6.0]  
>>> pairwiseHalfSums u  
[2.0,2.0,2.0,2.0,2.0,2.0,2.0,2.0,2.0]  
>>> pairwiseHalfSums x  
[5.0,5.5,5.0,5.5,5.0,4.5,5.0,4.5,5.0]  
>>> □
```

Task 7g – The pairwiseTermPairs function

Function Definition

--- pairwiseTermPairs

pairwiseTermPairs :: [Int] -> [(Int,Double)]

pairwiseTermPairs numbers = zip (pairwiseDifferences numbers) (pairwiseHalfSums numbers)

Demo

```
>>> pairwiseTermPairs a
[(-3,3.5),(4,3.0),(-2,2.0)]
>>> pairwiseTermPairs b
[(-2,2.0),(-3,4.5),(4,4.0),(-3,3.5)]
>>> pairwiseTermPairs c
[(0,4.0),(2,3.0),(1,1.5),(0,1.0),(-1,1.5),(0,2.0),(-2,3.0),(0,4.0),(-4,6.0)]
>>> pairwiseTermPairs u
[(0,2.0),(0,2.0),(0,2.0),(0,2.0),(0,2.0),(0,2.0),(0,2.0),(0,2.0),(0,2.0)]
>>> pairwiseTermPairs x
[(-8,5.0),(7,5.5),(-6,5.0),(5,5.5),(-4,5.0),(5,4.5),(-6,5.0),(7,4.5),(-8,5.0)]
>>> □
```

Task 7h – The pairwiseTerms functional

Function Definitions

--- term

term :: (Int,Double) -> Double

term ndPair = abs (fromIntegral (fst ndPair) / (snd ndPair))

--- pairwiseTerms

pairwiseTerms :: [Int] -> [Double]

pairwiseTerms numbers = map (term) (pairwiseTermPairs numbers)

Demo

```
>>> pairwiseTerms a  
[0.8571428571428571, 1.3333333333333333, 1.0]  
>>> pairwiseTerms b  
[1.0, 0.6666666666666666, 1.0, 0.8571428571428571]  
>>> pairwiseTerms c  
[0.0, 0.6666666666666666, 0.6666666666666666, 0.0, 0.6666666666666666, 0.0, 0.6666666666666666]  
>>> pairwiseTerms u  
[0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0]  
>>> pairwiseTerms x  
[1.6, 1.27272727272727, 1.2, 0.9090909090909091, 0.8, 1.11111111111112, 1.2, 1.5555555555556, 1.6]  
>>> □
```

Task 7i – The nPVI function

Function Definition

--- nPVI

nPVI :: [Int] -> Double

nPVI xs = normalizer xs * sum (pairwiseTerms xs)

where normalizer xs = 100 / fromIntegral ((length xs) - 1)

Demo

```
>>> nPVI a  
106.34920634920636  
>>> nPVI b  
38.09523809523809  
>>> nPVI c  
37.03703703703703  
>>> nPVI u  
0.0  
>>> nPVI x  
124.98316498316497  
>>> □
```

Task 8 – Historic Code: The Dit Dah Code

Subtask 8a

```
>>> dit  
"-"  
>>> dah  
"---"  
>>> (+++) "Hey" "there!"  
"Hey there!"  
>>> m  
('m', "--- ---")  
>>> g  
('g', "---- ----")  
>>> h  
('h', "---- -")  
>>> symbols  
[('a', "- ----"), ('b', "---- - - -"), ('c', "---- - ---- -"), ('d', "---- - - -"), ('e', "- -"), ('f', "---- - - - -"), ('g', "---- - - - -"), ('h', "---- - - - -"), ('i', "- - -"), ('j', "- - - - - - -"), ('k', "---- - - - -"), ('l', "---- - - - -"), ('m', "---- - - - -"), ('n', "---- - - - -"), ('o', "---- - - - - -"), ('p', "---- - - - - -"), ('q', "---- - - - - - -"), ('r', "---- - - - - -"), ('s', "---- - - - - -"), ('t', "---- - - - - -"), ('u', "---- - - - - -"), ('v', "---- - - - - - -"), ('w', "---- - - - - - -"), ('x', "---- - - - - - - -"), ('y', "---- - - - - - - - -"), ('z', "---- - - - - - - - -")]  
>>> □
```

Subtask 8b

```
>>> assoc 'c' symbols  
('c', "---- - - - -")  
>>> assoc 'z' symbols  
('z', "---- - - - - -")  
>>> find 'a'  
"- - -"  
>>> find 'b'  
"---- - - - -"  
>>> □
```

Subtask 8c

```
>>> addletter (find 'h') (find 'i')
"- - - - -"
>>> addword ( addletter (find 'h') (find 'i') ) ( addletter (find 'j') (find 'o') )
"- - - - - - - - - - - - - - -"
>>> droplast3 (addword ( addletter (find 'h') (find 'i') ) ( addletter (find 'j') (find 'o') ))
"- - - - - - - - - - - - -"
>>> droplast7 (addword ( addletter (find 'h') (find 'i') ) ( addletter (find 'j') (find 'o') ))
"- - - - - - - - - - -"
>>> []
```

Subtask 8d