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## Assignment: BNF Grammar

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Abstract: This assignment asked me to construct BNF grammars and parse trees for 5 languages. The 5 languages include Shapes, SQN (special quaternary numbers), fours, BXR (Boolean-expressions), and CF (color-fun).

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### Interaction: Shapes

#### Grammar:

<S> ::= ( <list> )

<list> ::= <el1><el2><el3><el4>

<el1> ::= ( <part1.1><part1.2> )

<el2> ::= ( <part2.1><part2.2> )

<el3> ::= ( <part3.1><part3.2> )

<el4> ::= ( <part4.1><part4.2> )

<part1.1> ::= size

< part1.2> ::= big | medium | small

< part2.1> ::= color

< part2.2> ::= red | blue | yellow

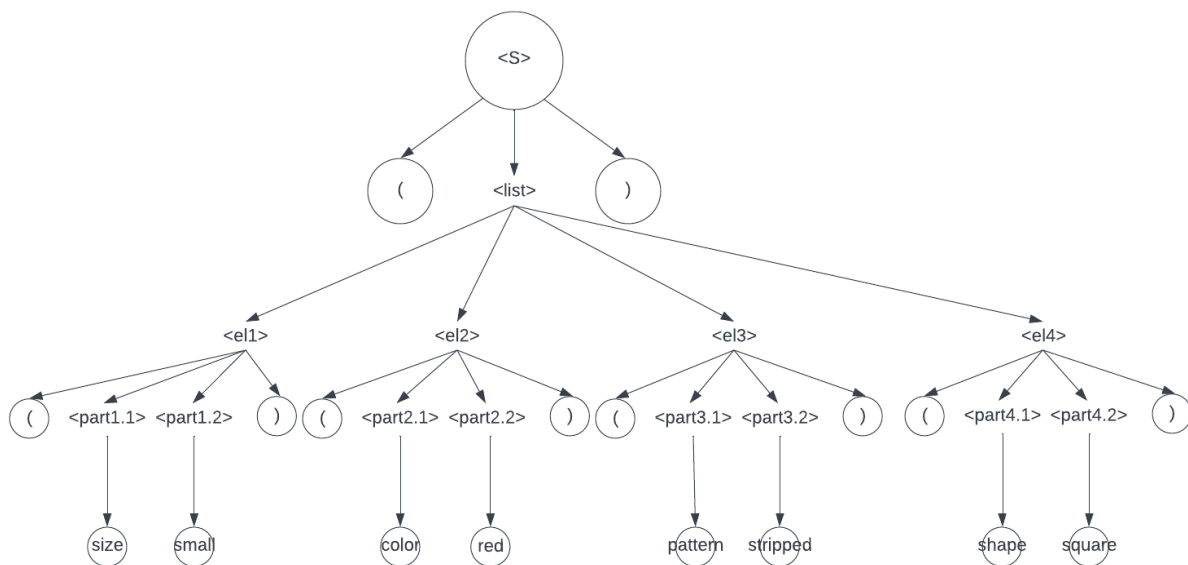
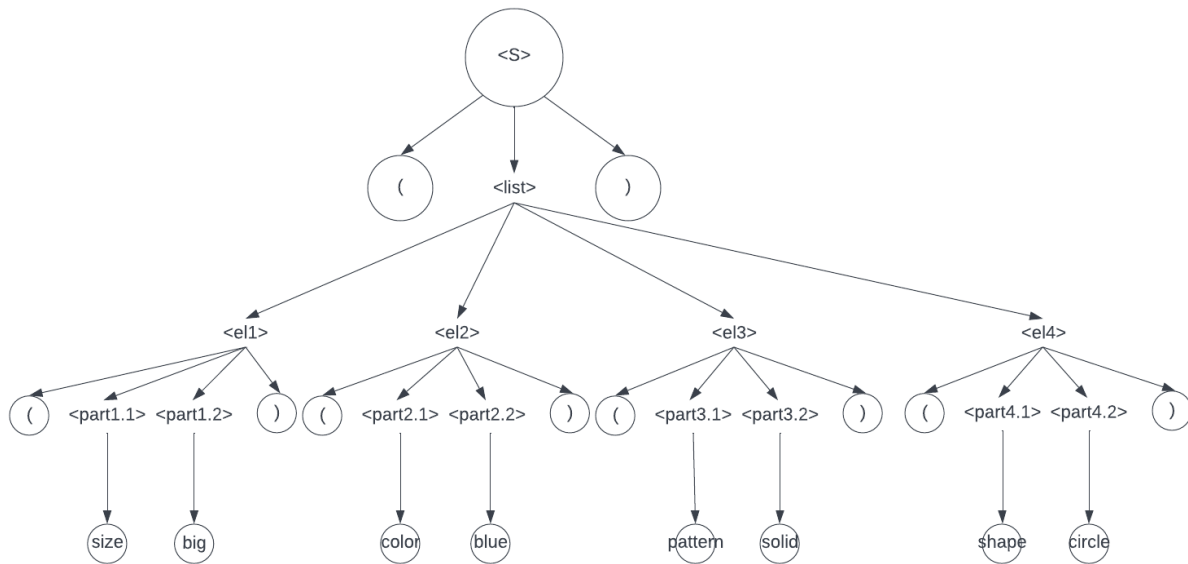
< part3.1> ::= pattern

< part3.2> ::= striped | dotted | solid

< part4.1> ::= shape

< part4.2> ::= circle | square | triangle

#### Parse Trees:




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## Interaction: SQN

### Grammar:

$\langle S \rangle ::= 0 \mid \langle \text{start-sequence} \rangle$

$\langle \text{start-sequence} \rangle ::= \langle 1\text{-digit} \rangle \mid \langle 2\text{-digit} \rangle \mid \langle 3\text{-digit} \rangle$

$\langle 0\text{-sequence} \rangle ::= \langle 1\text{-digit} \rangle \mid \langle 2\text{-digit} \rangle \mid \langle 3\text{-digit} \rangle \mid \langle \text{empty} \rangle$

$\langle 1\text{-sequence} \rangle ::= \langle 0\text{-digit} \rangle \mid \langle 2\text{-digit} \rangle \mid \langle 3\text{-digit} \rangle \mid \langle \text{empty} \rangle$

$\langle 2\text{-sequence} \rangle ::= \langle 0\text{-digit} \rangle \mid \langle 1\text{-digit} \rangle \mid \langle 3\text{-digit} \rangle \mid \langle \text{empty} \rangle$

$\langle 3\text{-sequence} \rangle ::= \langle 0\text{-digit} \rangle \mid \langle 1\text{-digit} \rangle \mid \langle 2\text{-digit} \rangle \mid \langle \text{empty} \rangle$

$\langle \text{empty} \rangle ::= \epsilon$

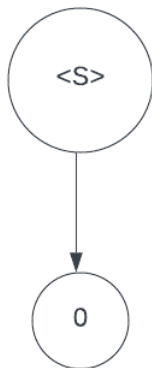
$\langle 0\text{-digit} \rangle ::= 0 \langle 0\text{-sequence} \rangle$

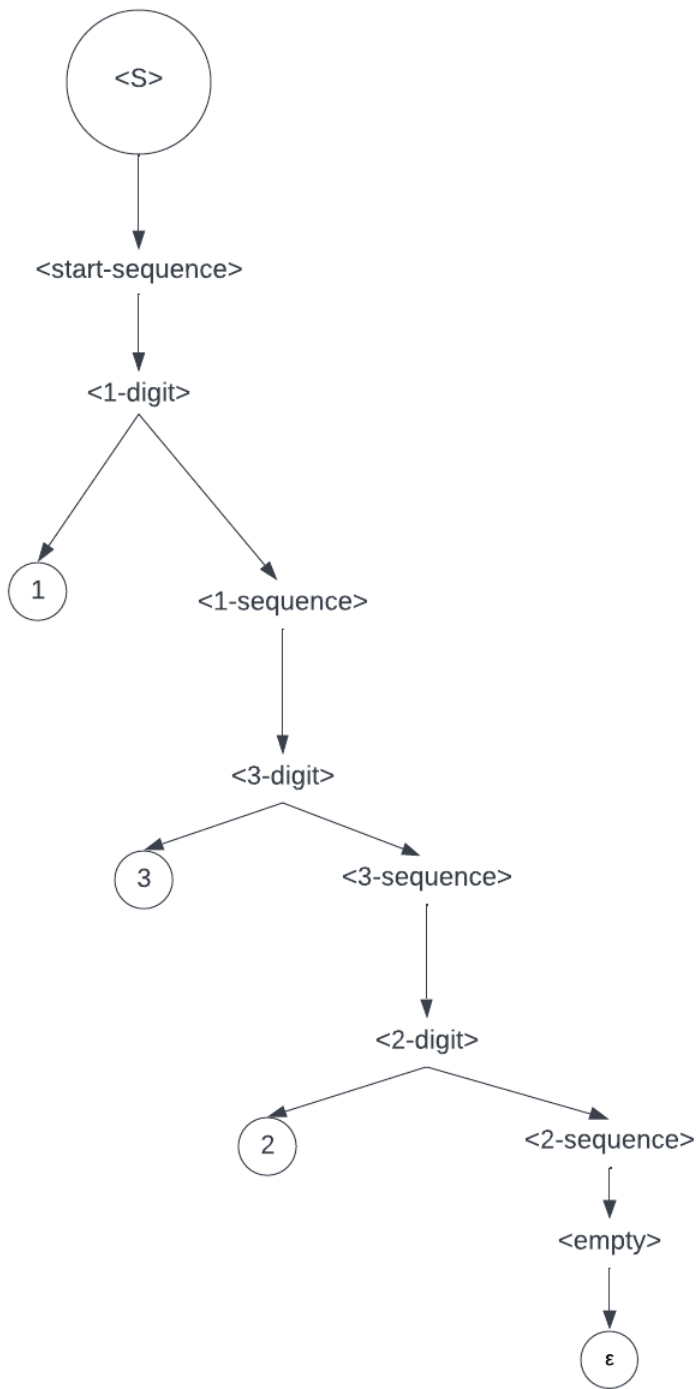
$\langle 1\text{-digit} \rangle ::= 1 \langle 1\text{-sequence} \rangle$

$\langle 2\text{-digit} \rangle ::= 2 \langle 2\text{-sequence} \rangle$

$\langle 3\text{-digit} \rangle ::= 3 \langle 3\text{-sequence} \rangle$

**Parse Trees:**





Explanation: Why 1223 is not available in the parse tree? Starting at the beginning of sequence we can only choose two options a 0 or a start sequence. The start sequence is the path we will follow which leads us into the next part which is to choose the “1-digit” non-terminal. This non-terminal gives us the 1 in the 1223 sequence and we look into the “1-sequence” non-terminal which has the option to pick “2-digit” to get us our 2 that we seek in the 1223 sequence. A second 2 is not allowed because the “2-

sequence" non-terminal has 4 options, "0-digit" to get a 0, "1-digit" to get a 1, "3-digit" to get a 3, and "empty" to stop the sequence.

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## Interaction: Fours

Grammar:

$\langle S \rangle ::= \langle \text{start-1s} \rangle \mid \langle \text{start-2s} \rangle \mid \langle \text{start-3s} \rangle \mid \langle \text{start-4s} \rangle$

$\langle \text{start-1s} \rangle ::= \langle 1s \rangle \langle 1\text{-seq} \rangle$

$\langle \text{start-2s} \rangle ::= \langle 2s \rangle \langle 2\text{-seq} \rangle$

$\langle \text{start-3s} \rangle ::= \langle 3s \rangle \langle 3\text{-seq} \rangle$

$\langle \text{start-4s} \rangle ::= \langle 4s \rangle \langle 4\text{-seq} \rangle$

$\langle 1\text{-seq} \rangle ::= \langle \text{start-1s} \rangle \mid \langle \text{start-2s} \rangle \mid \langle \text{start-3s} \rangle \mid \langle \text{start-4s} \rangle \mid \langle \text{empty} \rangle$

$\langle 2\text{-seq} \rangle ::= \langle \text{start-2s} \rangle \mid \langle \text{start-3s} \rangle \mid \langle \text{start-4s} \rangle \mid \langle \text{empty} \rangle$

$\langle 3\text{-seq} \rangle ::= \langle \text{start-3s} \rangle \mid \langle \text{start-4s} \rangle \mid \langle \text{empty} \rangle$

$\langle 4\text{-seq} \rangle ::= \langle \text{start-4s} \rangle \mid \langle \text{empty} \rangle$

$\langle \text{empty} \rangle ::= \epsilon$

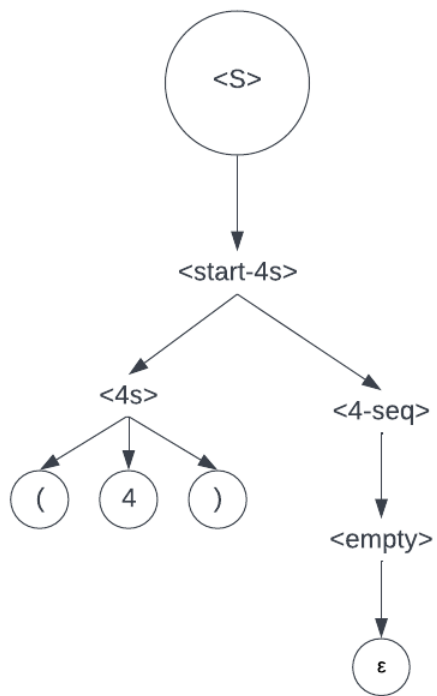
$\langle 1s \rangle ::= ( 1 1 1 1 )$

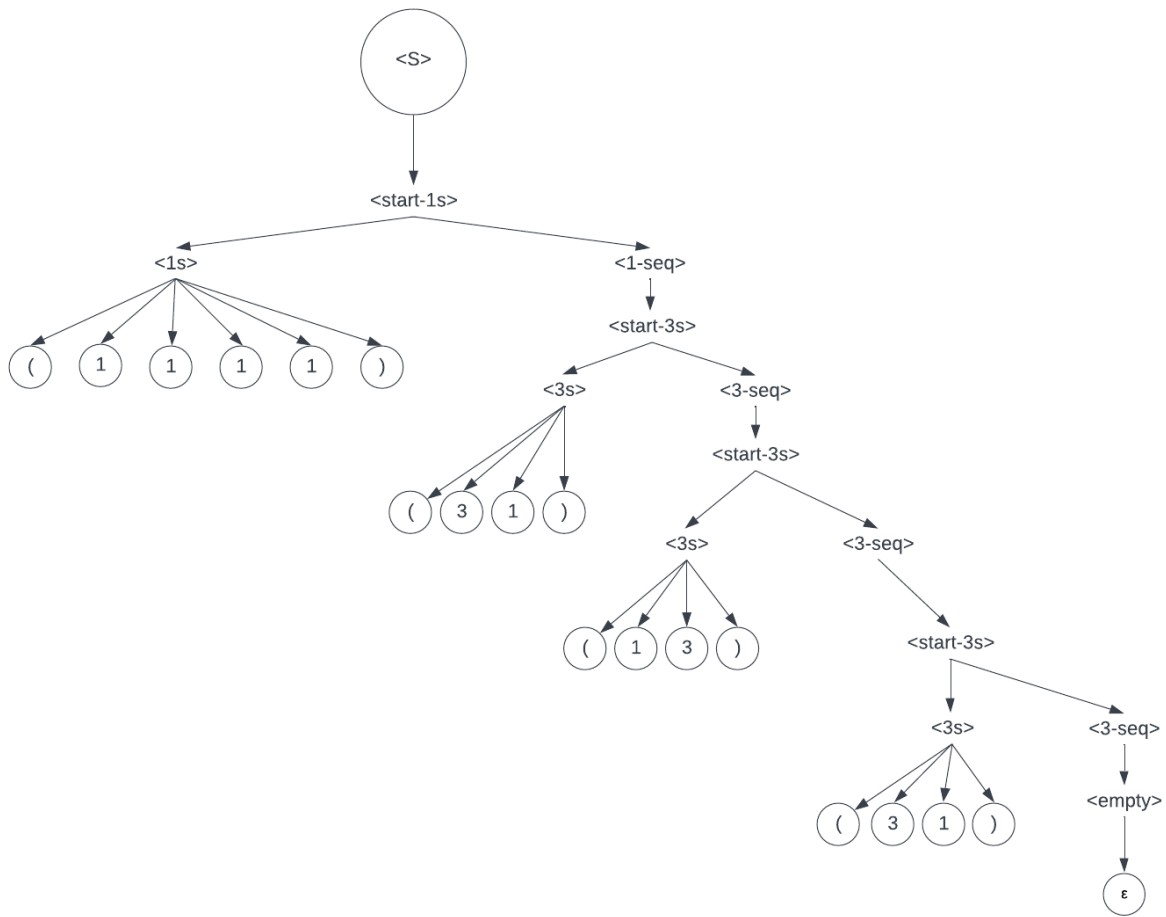
$\langle 2s \rangle ::= ( 1 1 2 ) \mid ( 1 2 1 ) \mid ( 2 1 1 )$

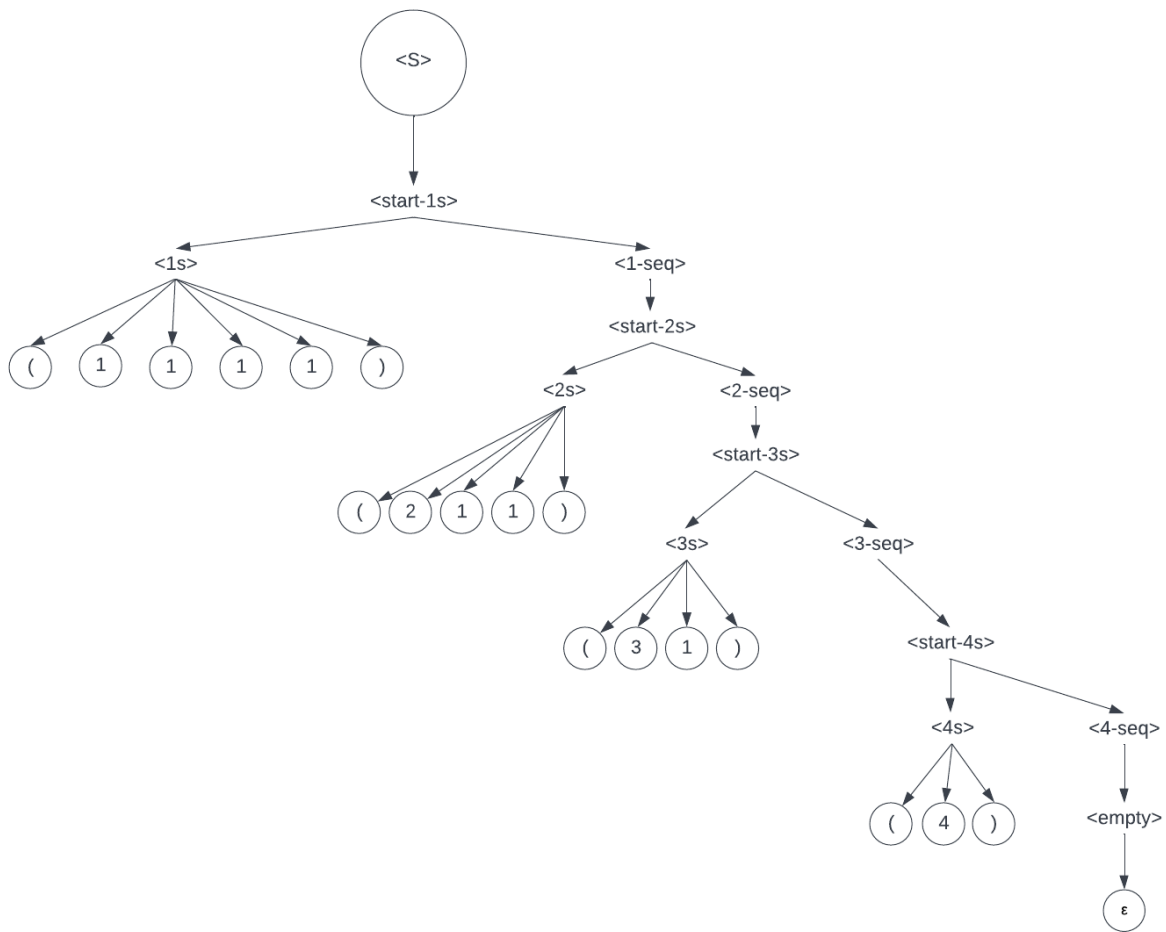
$\langle 3s \rangle ::= ( 3 1 ) \mid ( 1 3 )$

$\langle 4s \rangle ::= ( 4 )$

Parse Trees:








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## Interaction: BXR

### Grammar:

$\langle S \rangle ::= \langle \text{and} \rangle \mid \langle \text{or} \rangle \mid \langle \text{not} \rangle$

$\langle \text{and} \rangle ::= ( \text{ and } \langle \text{and-op-list} \rangle )$

$\langle \text{or} \rangle ::= ( \text{ or } \langle \text{or-op-list} \rangle )$

$\langle \text{not} \rangle ::= ( \text{ not } \langle \text{not-op-list} \rangle )$

$\langle \text{and-op-list} \rangle ::= \langle \text{value} \rangle \langle \text{and-op-list} \rangle \mid \langle \text{empty} \rangle$

$\langle \text{or-op-list} \rangle ::= \langle \text{value} \rangle \langle \text{or-op-list} \rangle \mid \langle \text{empty} \rangle$

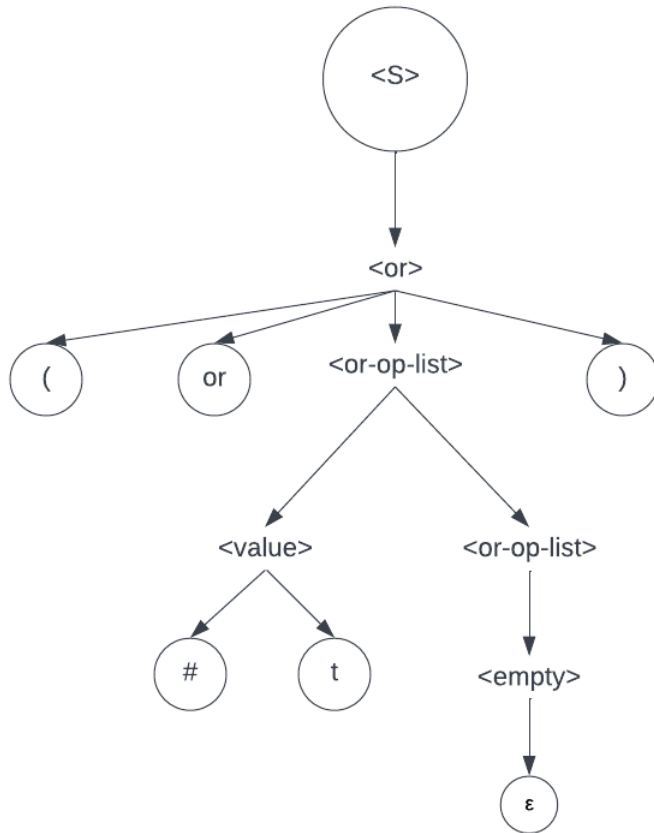
$\langle \text{not-op-list} \rangle ::= \langle \text{value} \rangle$

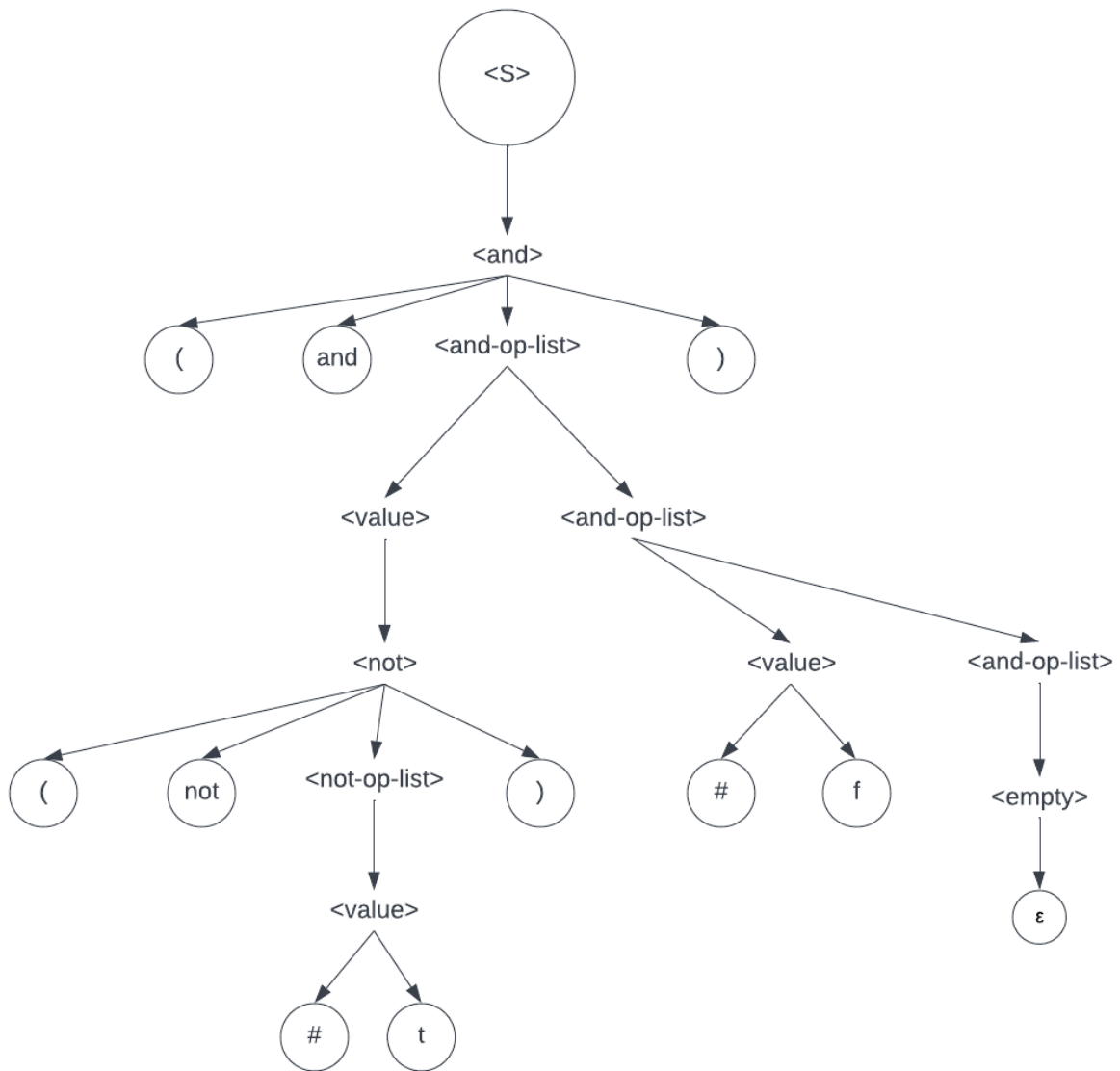
$\langle \text{empty} \rangle ::= \epsilon$



$\langle \text{value} \rangle ::= \#t \mid \#f \mid \langle \text{and} \rangle \mid \langle \text{or} \rangle \mid \langle \text{not} \rangle$

**Parse Trees:**






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## Interaction: CF

Grammar:

$\langle S \rangle ::= \langle \text{operators} \rangle$

$\langle \text{operators} \rangle ::= \langle \text{add} \rangle \mid \langle \text{show} \rangle \mid \langle \text{describe} \rangle \mid \langle \text{colors} \rangle$

$\langle \text{add} \rangle ::= \text{add } \langle \text{value} \rangle \langle \text{name} \rangle$

$\langle \text{show} \rangle ::= \text{show } \langle \text{name} \rangle$

$\langle \text{describe} \rangle ::= \text{describe } \langle \text{name} \rangle$

<colors> ::= colors

<value> ::= ( <rgb-value> <rgb-value> <rgb-value> ) | ( <rgb-value> <rgb-value> <rgb-value> <rgb-value> )

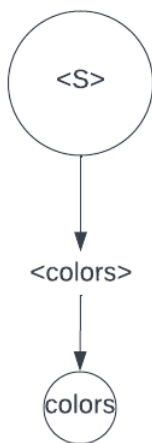
<name> ::= <string>

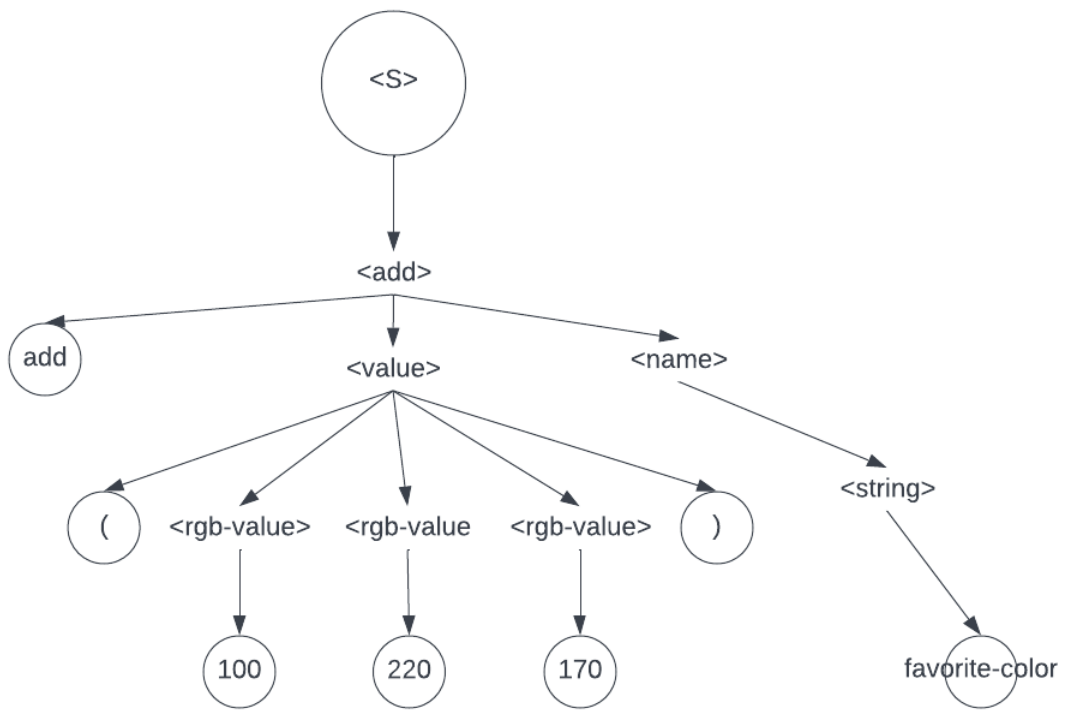
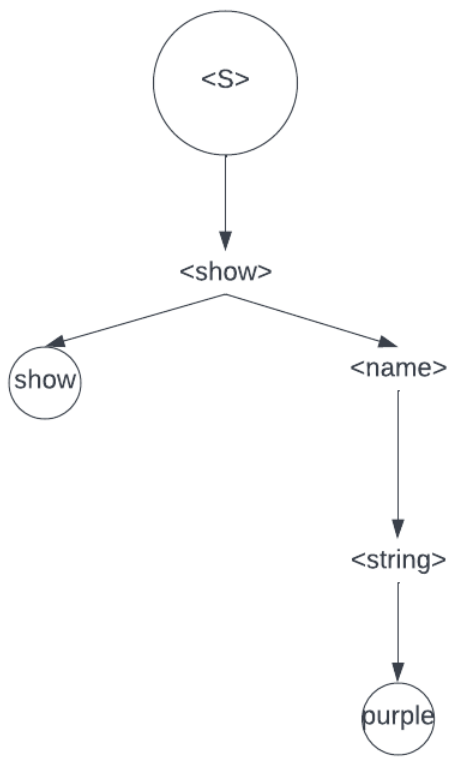
Dictionary:

<rgb-value> is defined as any integer value from 0 to 255.

<string> is defined as any sequence of characters.

Parse Trees:





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## Interaction: BNF?

What is BNF?

BNF is a way to describe a language that is easier to understand than using a natural language such as English. BNF is a notation that includes the start sequence, rules that define the language which include non-terminal and terminal symbols. When you draw parse-trees using the BNF it will show the reader what is a valid sentence in the language.